



AD FALCON API Manual

# Nonlinear Elasticity

Javad Ghorbani

March 14, 2026

## Contents

|          |                             |          |
|----------|-----------------------------|----------|
| <b>1</b> | <b>Nonlinear Elasticity</b> | <b>3</b> |
| 1.1      | Syntax . . . . .            | 3        |
| 1.1.1    | Bulk Modulus . . . . .      | 3        |
| 1.1.2    | Shear Modulus . . . . .     | 3        |



# 1 Nonlinear Elasticity

## 1.1 Syntax

This model is configured in % Materials as a user-defined mechanical material. Use @UMAT: with category Mechanical and pass the parameters as name=value pairs.

Example:

```
@UMAT: path/to/nonlinear_elastic.cpp path/to/nonlinear_elastic.hpp
Mechanical K0=400 G0=200 PATM=101325 P_min=1.0
```

The model employs two hypoelastic laws to describe the elastic behavior through bulk and shear moduli, characterized by  $K_0$  and  $G_0$  as the primary elasticity parameters.

### 1.1.1 Bulk Modulus

$$K = K_0 p_{atm} \frac{(1+e)}{e} \left( \frac{p'}{p_{atm}} \right)^{\frac{2}{3}} \quad (1)$$

### 1.1.2 Shear Modulus

$$G = G_0 p_{atm} \frac{(2.97 - e)^2}{1 + e} \left( \frac{p'}{p_{atm}} \right)^{\frac{1}{2}} \quad (2)$$